

Package: Qapprox (via r-universe)

August 22, 2024

Type Package

Title Approximation to the Survival Functions of Quadratic Forms of Gaussian Variables

Version 0.2.0

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Description Calculates the right-tail probability of quadratic forms of Gaussian variables using the skewness-kurtosis ratio matching method, modified Liu-Tang-Zhang method and Satterthwaite-Welch method. The technical details can be found in Hong Zhang, Judong Shen and Zheyang Wu (2020) [<arXiv:2005.00905>](https://arxiv.org/abs/2005.00905).

License GPL-2

Imports stats

Encoding UTF-8

RoxygenNote 6.1.0

NeedsCompilation no

Date/Publication 2021-07-07 04:30:05 UTC

Repository <https://wpihongzhang.r-universe.dev>

RemoteUrl <https://github.com/cran/Qapprox>

RemoteRef HEAD

RemoteSha 0d993a7b6cde038b67d6b97a0b47701db24aca40

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Description

Right-tail probability of quadratic forms of centered Gaussian variables.

Usage

```
Qapprox(q, Sigma, A = NULL, method = "MR")
```

Arguments

| | |
|---------------|---|
| <i>q</i> | - quantile, could be a vector. |
| <i>Sigma</i> | - covariance matrix of Gaussian variables. |
| <i>A</i> | - a positive-semi-definite matrix that defines the quadratic form. |
| <i>method</i> | - "MR": moment-ratio (skewness-kurtosis) matching method; "SW": Satterthwaite-Welch method that matches mean and variance; "LTZ4": Liu-Tang-Zhang method that matches the kurtosis. |

Value

The right-tail probability of a quadratic form ($Q = X'AX$) of centered Gaussian variables.

References

1. Hong Zhang, Judong Shen and Zheyang Wu. "An efficient and accurate approximation to the distribution of quadratic forms of Gaussian variables", arXiv:2005.00905.

Examples

```
n <- 100
Sigma <- toeplitz(1/(1:n))
thr <- 180
Qapprox(thr, Sigma, method="SW")
Qapprox(thr, Sigma, method="LTZ4")
Qapprox(thr, Sigma, method="MR")
```

| | |
|------------|--|
| Qapprox_nc | <i>Right-tail probability of quadratic forms ($Q = X'AX$) of noncentral Gaussian variables.</i> |
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Description

Right-tail probability of quadratic forms ($Q = X'AX$) of noncentral Gaussian variables.

Usage

```
Qapprox_nc(q, mu, Sigma, A = NULL, method = "MR")
```

Arguments

| | |
|--------|---|
| q | - quantile, could be a vector. |
| mu | - mean vector of Gaussian variables. |
| Sigma | - covariance matrix of Gaussian variables. |
| A | - a positive-semi-definite matrix that defines the quadratic form. |
| method | - "MR": moment-ratio (skewness-kurtosis) matching method; "SW": Satterthwaite-Welch method that matches mean and variance; "LTZ4": Liu-Tang-Zhang method that matches the kurtosis. |

Value

The right-tail probability of a quadratic form ($Q = X'AX$) of noncentral Gaussian variables.

References

1. Hong Zhang, Judong Shen and Zheyang Wu. "An efficient and accurate approximation to the distribution of quadratic forms of Gaussian variables", arXiv:2005.00905.

Examples

```
n <- 100
Sigma <- toeplitz(1/(1:n))
mu <- rep(1, n)
thr <- 500
Qapprox_nc(thr, mu, Sigma, method="SW")
Qapprox_nc(thr, mu, Sigma, method="LTZ4")
Qapprox_nc(thr, mu, Sigma, method="MR")
```

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